

# Deciding Between Conflicting Influences

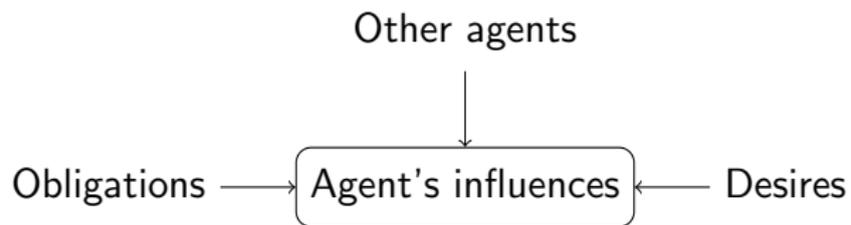
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# Conflicts in decision making



# Conflicts in decision making

The agent's influences:

- Eat breakfast (Desire)
- Go to work (Obligation)
- Take a vacation (Desire)

How can the agent choose between the conflicting influences?

# Conflicts in decision making

**Simple solution:** A priori ordering.

- Desires before obligations  $\rightarrow$  *Selfish agent*
- Obligations before desires  $\rightarrow$  *Social agent*

**Better:** Consequences of being in different situations

- $\neg work \rightarrow fired$
- $work \rightarrow \neg fired$

## Rule-based preferences

Agent's preferences and expectations represented as simple *if X then Y* rules.

- If it rains, then I prefer to drive to work  $\rightarrow (rains, drive)$
- If I feel sick, then I normally stay at home  $\rightarrow (sick, stay\_home)$
- If I go to work, then I prefer to leave early  $\rightarrow (work, leave\_early)$
- If I am late for work, then I normally do not leave early  $\rightarrow (late, \neg leave\_early)$

# The approach

- A model satisfying the rules.
- Using rules of the form  $(X, Y)$  in the agent's decision process
  - Preference rules
  - Expectation rules
- Most preferred states
- Tolerable states

# Semantics of the Rules

$(\varphi, \psi) \equiv \text{if } \varphi \text{ then (preferably/normally) } \psi$

- (a)  $\varphi$  is never true.
- (b)  $\psi$  is true in more favored  $\varphi$ -worlds.

We assume the agent's intention of the preference is that  $\varphi$  is sometimes true.

# A running example

$$Alice = \{ (\top, \neg snow), (snow, \neg work), \\ (\top, \neg fired), (work, leave\ early) \}$$

$$Expectations = \{ (\top, work), (snow, \neg fired \mathbf{and} \neg work), \\ (\neg snow \mathbf{and} \neg work, fired), \\ (\top, \neg leave\ early), (work, \neg fired) \}$$

## Applying the rules

An agent specifies a set of rules  $(\varphi, \psi)$ . Given worlds  $w_1$  and  $w_2$ :

- $w_1 \models \varphi \wedge \psi$ ,
- $w_2 \models \varphi \wedge \neg\psi$ .

According to the agent,  $w_1$  is preferred over  $w_2$ ,  $w_1 \leq w_2$ .

Given rule  $(snow, \neg work)$ ,  $w_1$  and  $w_2$  are then:

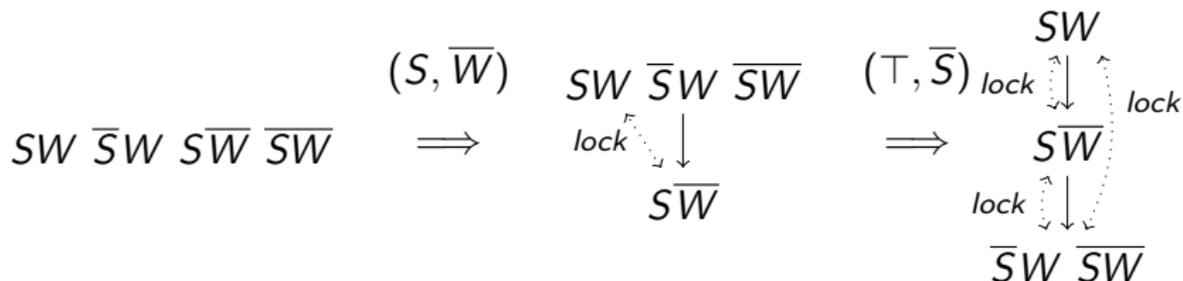
- $w_1 \models snow \wedge \neg work$
- $w_2 \models snow \wedge work$

# Ordering the possible worlds

- Each world is mapped to a natural number, an  $o$ -value.
- An ordering  $\leq$  orders the worlds in  $W$  in descending order according to their  $o$ -value.
- Initially  $o(w) = 0$  for all worlds in  $W$ .

# Example

$$\text{Alice} = \{(snow, \neg work), (\top, \neg snow)\}$$



$$S\bar{W} \leq SW$$

# Preserving applied rules

**Proposition.** Given an initial ordering  $\leq$ , a set of rules  $\mathcal{R} = \{r_1, \dots, r_n\}$  where each  $r_i$  is of the form  $(\varphi_i, \psi_i)$ , the result of successfully applying rules  $r_1$  to  $r_i$ ,  $0 < i \leq n$  is an ordering which respects rules  $\{r_1, \dots, r_i\}$ .

# Minimizing locked worlds

Notice that  $(snow, \neg work)$  was applied before  $(\top, \neg snow)$ .

The less propositions in a rule, the more general it is.

Each rule receives a value depending on its generality.

- ①  $(snow, \neg fired \text{ and } \neg work)$
  - ②  $(snow, \neg work)$
  - ③  $(\top, \neg snow)$
- ↓ More general

More specialized rules are applied first.

# Making a decision

- The ordering respects the agent's rules
- How should the agent choose between influences?
  - Preferred worlds
  - Tolerable consequences

# Qualitative Decision Theory

- The Logic for Qualitative Decision Theory (Boutilier) orders worlds according to preference and normality.
- $I(B \mid A) \equiv$  *If A then ideally B*
- $T(B \mid A) \equiv \neg I(\neg B \mid A)$
- $A \leq_P B \equiv$  *A is at least as preferred as B*
- $A \Rightarrow B \equiv$  *If A then normally B*

## Expected consequence

- A consequence of an action must be something *controllable*.
  - *The weather?*
  - *Taking the car to work?*
  - *Getting fired?*
- An agent  $i$  has a set of controllable propositions  $C(i)$ .
- The expected consequence(s) of bringing about  $\varphi$  is then:

$$EC_i(\varphi) = \{C_\varphi \mid (B(i) \wedge \varphi \Rightarrow C_\varphi) \text{ where } C_\varphi \in C(i)\}$$

# Making a decision

The best decision the agent  $i$  can make is then  $Dec(i)$ , which is:

- The influence that is most preferred, or (if more than one)
- the influence(s) with most tolerable consequences.

# The agent can always do something

**Proposition.** Given an agent  $i$ , a non-empty set of influences  $F(i)$  and the expected consequences  $EC_i(\varphi)$  for all  $\varphi \in F(i)$ , the set of decisions,  $Dec(i)$  is always non-empty.

## Back to Alice...

- The setup:

$$Alice = \{(\top, \bar{S}), (S, \bar{W}), (\top, \bar{F}), (W, E)\}$$

$$Expectations = \{(\top, W), (S, \bar{FW}), (\bar{SW}, F), (\top, \bar{E}), (W, \bar{F})\}.$$

- Influences

- Doesn't want to work:  $\neg work$
- Ought to go to work:  $work$

- Alice's influences are then  $F(a) = \{work, \neg work\}$ .

## It is snowing

$$F(a) = \{W, \overline{W}\}$$

Alice's preferences

 $\overline{EFSW} \quad \overline{EFSW} \quad \overline{EFSW}$ 

 $\overline{EFSW}$ 

 $\overline{EFSW}$ 

 $\overline{EFSW}$ 

 $\overline{EFSW} \quad \overline{EFSW}$ 

Expectation

 $\overline{EFSW} \quad \overline{EFSW} \quad \overline{EFSW} \quad \overline{EFSW}$ 

 $\overline{EFSW}$ 

 $\overline{EFSW} \quad \overline{EFSW}$ 

 $\overline{EFSW}$ 

$$Dec(a) = \{\overline{W}\}$$

# It is not snowing

$$F(a) = \{W, \overline{W}\}$$

Alice's preferences

$\overline{EFSW}$   $\overline{EFSW}$   $\overline{EFSW}$



$\overline{EFSW}$



$\overline{EFSW}$



$\overline{EFSW}$



$\overline{EFSW}$   $\overline{EFSW}$

Expectation

$\overline{EFSW}$   $\overline{EFSW}$   $\overline{EFSW}$   $\overline{EFSW}$



$\overline{EFSW}$



$\overline{EFSW}$   $\overline{EFSW}$



$\overline{EFSW}$

$$Dec(a) = \{W\}$$

# “Social” or “Selfish”?

- In some cases the agent violates its obligation.
- In other cases it ignores its desire.

## Conclusion & Future work

- Conflicts arise in the agent deliberation process
- Rules of preference and expectation are specified
- Model generation
- Conflicts resolved using expected consequences
- No labeling of 'social' or 'selfish' agents

### Future work

- Optimizing model generation
- Using predicates in rules

Thank you for your attention